



## Population growth

How can there be so many @&X!! mosquitoes?

## Lecture outline

- Two models of population growth
- Little  $r$
- Exponential population growth
- Logistic population growth
- Density-dependent regulation of populations

## Modeling population growth

- Depends on how organisms reproduce
  - In a discrete, non-overlapping way, often called \_\_\_\_\_ growth
  - In a continuous, overlapping way
- Either way, populations only change in abundance because of four parameters...
- Nevertheless, we often assume a *closed* population, which means we ignore...

$r$

- At any moment in time, an individual's contribution to population growth is modelled as the per capita or intrinsic or instantaneous rate of increase

- $r =$  \_\_\_\_\_

- $b =$  \_\_\_\_\_ / \_\_\_\_\_

- $d =$  \_\_\_\_\_ / \_\_\_\_\_

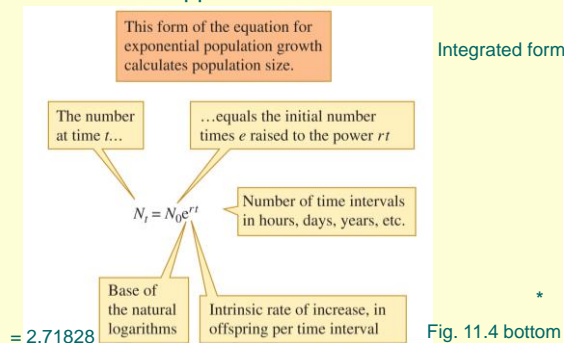
Species	$r$	Doubling time
<i>E. coli</i>	58.7	17 min
<i>Paramecium</i>	1.59	10.5 hr
<i>Tribolium</i>	0.101	6.9 days
<i>Rattus</i>	0.015	46.8 days
<i>Bos</i>	0.001	1.9 yr
<i>Nothofagus</i>	0.000075	25.3 yr

- If  $r > 0$ , population is ?
- If  $r = 0$ , population is ?
- If  $r < 0$ , population is ?

From Gotelli

## One equation for exponential growth

- When is this applicable?



## Exponential growth in nature



*Grus americana*

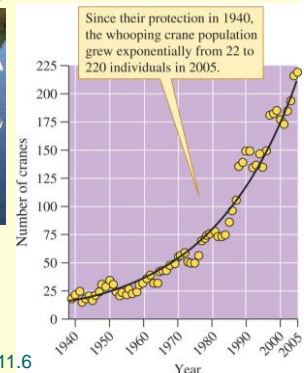
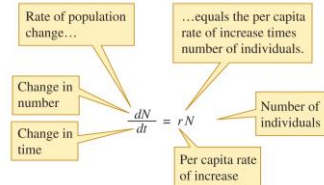


Fig. 11.6

## A second exponential equation

- Instead of just looking at the total number of individuals, we can also express exponential growth as the rate of change in population size

This form of the equation for exponential population growth expresses the rate of population change as the product of  $r$  and  $N$ .



Differential form

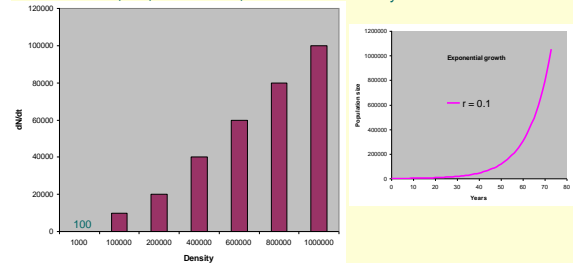
Fig. 11.4 top

## Differential form in action

- $r = 0.1$

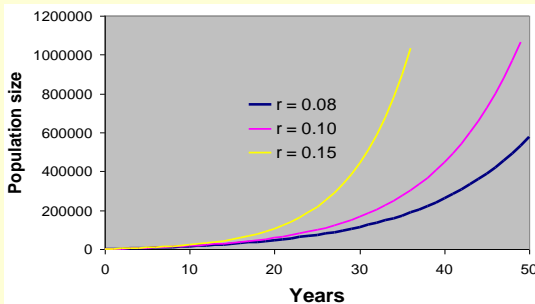
- at  $N = 1,000$ , add 100 individuals each year
- at  $N = 100,000$  add 10,000 individuals each year
- at  $N = 1,000,000$  add 100,000 individuals each year

$$\frac{dN}{dt} = rN$$



## Importance of magnitude of $r$

- $r = 0.08, 0.1, \text{ or } 0.15$ ;  $N_0 = 1000$ ;  $t = 1 \text{ yr}$ ; 1000 new immigrants each year, too (total = 36,000 to 50,000); note shape



## Is exponential growth always realistic?

- Why or why not?

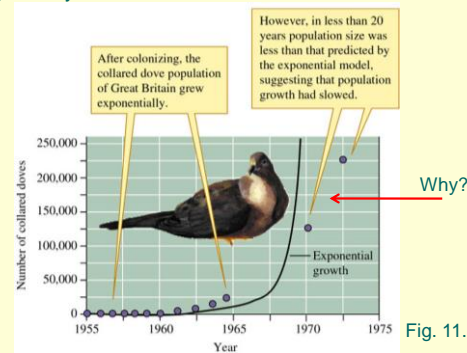
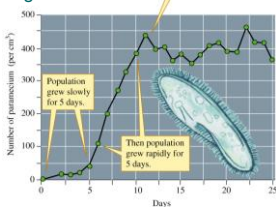


Fig. 11.7

## Logistic growth in the lab and field

Fig. 11.10



*Paramecium caudatum* in the lab  
Gause (1934)

Northern elephant seal in CA

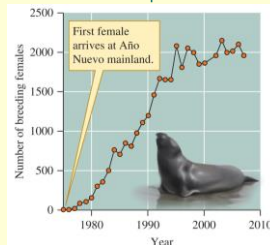


Fig. 11.12

## Logistic growth

- Shape?

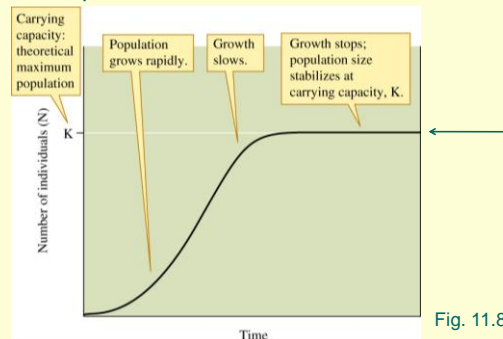


Fig. 11.8

## What is K?

### • Medium ground finch

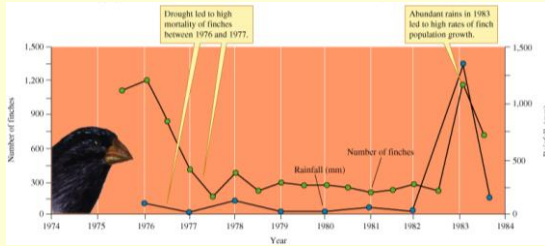


Fig. 11.17

## Logistic growth

### • Shape?

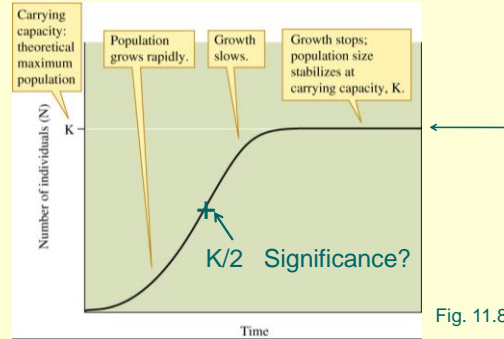
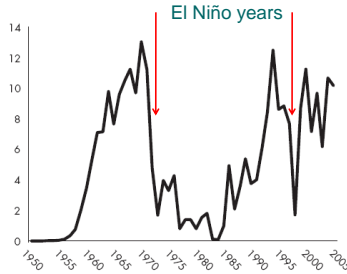


Fig. 11.8

## Optimal yield

Figure 4 Catches of Peruvian anchovy  
Million tonnes



Source: FAO Fisheries Database



Hannesson 2008

## Logistic growth equation

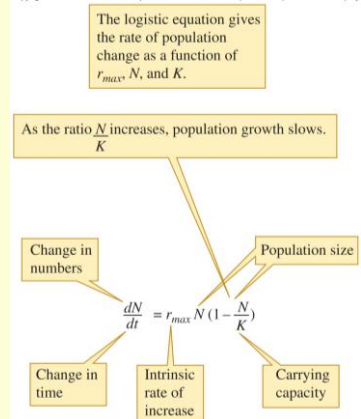


Fig. 11.13

## Population regulation

- $K$  is thought to be an **equilibrium density** and is maintained by **density-dependent regulation**
  - As population size changes, birth and death rates change, too
- So, for a population to be regulated at this equilibrium, it must be controlled by **density-dependent factors**

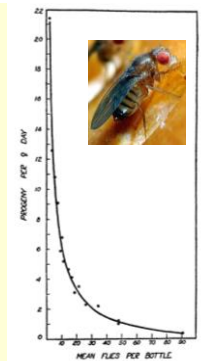


FIG. 10. SHOWING CHANGE IN RATE OF REPRODUCTION OF *DROSOPHILA* WITH INCREASING DENSITY OF THE MAJOR POPULATION. The circles give the observations and the smooth curve is the graph of the logistic equation discussed in the text.

Pearl (1927)

## What are some factors affecting population size?



Which ones are "density dependent" factors?



Which ones are "density independent"?

